Microfluidic sorting of arbitrary cells with dynamic optical tweezers

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Optical gradient forces generated by fast steerable optical tweezers are highly effective for sorting small populations of cells in a lab-on-a-chip environment. The presented system can sort a broad range of different biological specimens by an automated optimisation of the tweezer path and velocity profile. The optimal grab positions for subsequent trap and cell displacements are estimated from the intensity of the bright field image, which is derived theoretically and proven experimentally. We exhibit rapid displacements of 2 µm small mitochondria, yeast cells, rod-shaped bacteria and 30 µm large protoplasts. Reliable sorting of yeast cells in a microfluidic chamber by both morphological criteria and by fluorescence emission is demonstrated.

Introduction

For many years, fluorescence-activated cell sorting (FACS) has been the standard technique for sorting biological cells in suspension, featuring high throughput, purity, and yield. Besides the problem that available FACS machines are expensive and demanding to operate, the large numbers of cells needed for calibration and a sometimes lethal stress induced to the cells by shear forces limit the field of applications. Lab-on-a-chip systems promise to overcome this drawback. Existing microfluidic cell sorters operate either via redirecting flow (electro-osmosis or valves) or a magnetic, dielectrophoretic or optical forces acting directly on cells or on a droplet encapsulating them.

Laser optical actuation is especially advantageous, since properly chosen forces are strong enough, but usually non-damaging. Furthermore, spatial light distributions can be switched rapidly in intensity and shape, such that the microfluidic chip does not need any electrodes or active layers – in contrast to systems based on dielectrophoresis. Avoidance of cell encapsulation facilitates further investigation and recultivation.

All cell sorters exploiting optical forces which have been presented so far are designed for cells with a specific shape and size. Passive optical cell sorters use a specifically designed static light distribution, typically an optical lattice with a designed grating width to deflect cells in a microfluidic channel. Passive sorters can only sort by differences in refractive index, in size or in shape. In contrast, active optical sorters are able to sort nearly identical cells according to small differences in features, which are typically encoded by a spatial fluorescence distribution. Existing active optical sorters work with moderately focused beams, which are intensity modulated but not displaced. In both the passive and active sorting modes, force fields are distributed over a larger area and depend on the size and refractive index of the suspended objects. Hence, objects varying in these two parameters cannot be sorted without redesigning the system. In contrast, an optical point trap from a highly focused laser beam, also known as optical tweezers, produces significantly higher optical forces when the same laser power is applied to the cell.

In this paper, we present an optical particle sorter that uses rapid steerable optical traps to displace cells within a laminar flow inside a microchannel. Cells not grabbed by the optical tweezers stream into a different reservoir than those actively displaced to a parallel streamline. The system is preferably suitable for small populations of a few hundred or thousand cells or for sorting out rare events. A similar system has been realized only recently for a specific type of cell. However, our sorter can handle arbitrary cells since neither channel structure nor the forces of the optical tweezers need to be changed for a specific kind of cell. The optimal grab position for each specific cell can be determined by the intensity of bright field CCD images. In this paper, we derive and explain the relation between the bright field intensity and the expected optical force. Based on this information, an optimized optical trap path can be generated ensuring a rapid and secure displacement of each cell within the channel. Before activation of the optical trap, each cell can be classified by a bright field or a fluorescence image with 300 nm optical resolution, allowing sorting also by morphological criteria and expression of fluorescent markers. Moreover, an optically transparent microfluidic chamber suitable for mass production is used. The system is designed as an add-on for a...
standard inverted microscope and thus can be run in any standard lab.

The sorter’s capabilities are demonstrated in the first place by displacements of mitochondria, bacteria, yeast, and plant protoplasts at various displacement speeds or frequencies. In addition, a population of yeast cells is sorted inside a microchannel, where cells are classified by both their size and their fluorescence intensity in the same run.

**Experimental**

**Optical system**

The setup of the sorter (Fig. 1) uses an inverted microscope (Zeiss, Axiovert 200) as a platform. The objective lens (Zeiss, C-Apochromat, 40×, NA 1.2) is a coverslip-corrected water immersion lens and is used for imaging and focusing of the trapping laser, which operates in the near-infrared at 1064 nm (Alphalas Lasers, Monopower-1064-10W-SM). Images are captured with a CCD camera (Prosilica, GC1350H) with a full frame rate of 12.9 fps. An additional telescope system (0.5×) in front of the camera leads to an overall magnification of 20×. Fluorescence is excited with a mercury lamp (Zeiss, HXP120) during the integration time of the CCD; bright field images are illuminated software-triggered by a LED (Lumileds, Luxeon I). Both channels can be overlaid in the software’s camera window. The focused laser forming the optical trap is steered in its position in two dimensions by galvanometric mirrors (GSI, VM500+) deflecting the collimated laser in a plane conjugate to the pupil plane of the objective lens. After having received their signals by a D/A card (National Instruments, PCIe-6259), the mirrors can deflect at a 200 µs response and at 1 µs temporal resolution. The optical power in the focal plane was 270 mW for experiments with different cells on the piezo stage and 67 mW for sorting of yeast cells in the microchannel.

This arrangement is sketched in Fig. 1. It enables classification of cells (i) by the feature information delivered by bright field images, such as size, shape or more complex morphology, (ii) by the intensity of fluorescence light, or (iii) both. A logical flow diagram for this last option is shown in Fig. 1e. Only if a cell is classified positive in a fluorescence image (feature ii) and in the subsequent bright field image (feature i) is it localized precisely and moved by the optical trap to a streamline directed towards the channel for sorted cells.

**Microfluidic system**

The microfluidic sorting chip can be produced with technologies suitable for rapid prototyping and mass production. For the experiments presented here a prototype was used. Channels of 100 µm in width and 80 µm in height were precision milled in 1.5 mm thick Cyclic Olefin Copolymer (COC) 5013 (Fig. 1a). Inlets and outlets were drilled with a diameter of 0.5 mm. The chip was covered with a 140 µm thick foil of COC 8007, serving as the bottom of the channel. For sealing, both parts were cleaned with isopropanol and deionized water, exposed to cyclohexane vapour for 130 s, and subsequently pressed against each other with a hard rubber roll. The prototype was put into an aluminium frame and connected to a multichannel syringe pump (Cetoni, neMESYS) and output reservoirs (Eppendorf tube) via fittings and tubing (Upchurch Scientific, PEEK, 1/16” OD, 170 µm ID) (Fig. 1b,c).

**Cell preparation**

Mitochondria from fresh murine liver tissue was prepared as described earlier. Mitochondria are roundish cell organelles of about 2 µm diameter, have a membrane and are called cells throughout the rest of this paper. *Bacillus subtilis* are rod-shaped bacteria with a diameter of about 1 µm and a length of about 4 µm (for preparation see ref. 23).

![Fig. 1](a) Cells within the microchannel can be localized and classified with bright field (green) and/or fluorescence (blue) illumination through a high NA objective. Once a cell is classified, it is moved by optical tweezers (red) to a streamline of laminar flow which leads to the outlet for sorted cells. (b,c) Photographs of microfluidic chamber inserted into its chip holder and connected to tubing. (d) Fluid flow diagram with 3 inlets (blue) and 2 outlets (red). (e) Logical flow diagram for a popular sorting mode: 1. classification by the intensity in the fluorescence channel; 2. Additional classification by the size in the bright field channel. After positive classification, the bright field image is used to determine the location for the most efficient manipulation.
Protoplasts from the root of *Arabidopsis thaliana* with a diameter of 40 μm were chosen for the experiments (for preparation see ref. 24).

Yeast cells (*Saccharomyces cerevisiae*) were stained with MitoTracker Green (Invitrogen) as described in the manual, but with a five times higher concentration of stock solution. Stained and unstained suspensions were mixed in a 1:1 ratio, yielding a concentration of 4 × 10^7 cells per microliter.

Viability tests with Trypan Blue (Sigma Aldrich) were performed on a population immediately extracted after sorting and on an unsorted control group by counting under the microscope.

### Determination of the optimal trap path

Optical trapping forces are mainly dominated by the optical gradient force (dipole force), whereas the disadvantageous scattering force (radiation pressure) is to be minimized. At laser powers of about 100 mW, optical tweezers operated at λ = 1.06 μm can exert optical forces of 10–300 pN, depending on the polarisability α of the particle or of a part of the cell. A cell can then be moved through the medium by the trap as long as the optical gradient force is at least as high as the viscous drag force, F_{opt} ≥ F_d, which depends on its size and the drag speed. For an efficient displacement of a cell to another fluid stream line, it is essential to grab the cell at a suitable position and displace it as fast as possible in a minimal period of time.

In order to find an efficient grab location with maximal gradient force, information extracted from bright field images can be used.

The optical gradient force $F_{grad}$ on a volume $V$ of dipoles at position $b$ can be described with

$$F_{grad}(b) = \frac{1}{2\epsilon_0} \text{Re} \int V \left( \alpha(b) n^2(b) \nabla I_i(b) \right) dV$$

where $c$ is the speed of light and $\epsilon_0$ the vacuum permittivity. The polarisability $\alpha$, the refractive index $n$ and the incident intensity of the trapping light $I_i$ all vary with $b$. If we neglect absorption ($\alpha$ and $n$ real) and approximate the extent of the trapping focus or the trapped particle to be small, the integral in eqn (1) can be omitted, such that eqn (2) is valid.

With the Clausius-Mossotti relationship, the polarisability can be written as $\alpha(b) = (n^2(b) - (n(b) + \Delta n(b))^2)/(n^2(b) + 2(n(b) + \Delta n(b))^2)$, where $\Delta n$ is the difference of the refractive index to a neighboring position $b + \Delta b$. After a 1st order Taylor approximation of $\alpha$ around $\Delta n = 0$, we find $\alpha \approx 2\Delta n(3n)$ such that the optical gradient force can be written as

$$F_{grad}(b) \approx \frac{n(b)}{3\epsilon_0} \Delta n(b) \nabla I_i(b)$$

which means that $F_{grad}$ is approximately proportional to the local change of the refractive index $\Delta n$ at position $b$.

The spatial variation $\Delta n$ can be extracted from bright field images. For spatially coherent illumination (Koehler aperture closed), we get an interference pattern directly behind the focal plane described by:

$$\Delta I(b) = \Delta I_i(b) + \Delta I_s(b) + 2\sqrt{\Delta I_i(b)\Delta I_s(b) \cos(\Delta\Phi(b,0))}$$

where $\Delta I$ is the bright field intensity, $\Delta I_i$ the incident intensity, $\Delta I_s$ the scattered intensity, and $\Delta\Phi$ the phase shift between the two waves inside the volume element $V$. It is a complex task to determine the intensity within a thick, scattering cell. But for positions close to the cell membrane, where $\Delta n$ are maximal, it can be assumed that the light’s incidence angle and the emergent angle of the reflected light are both perpendicular to the cell’s normal in the focal plane, such that $\theta_l \approx \theta_i \approx 90^\circ$ and therewith $\Delta\Phi \approx \pi$ and $\cos(\Delta\Phi(0)) \approx -1$. Inserting $\Delta I_s = \Delta I_d^2$, into eqn (4) where $r_d(\Delta\Phi)$ is the reflection coefficient, we find:

$$\Delta I(b) = \Delta I_i(b)(1 - r_d)^2$$

Again, for large angles, the reflection coefficient can be simplified to $r_d \approx \Delta n(\Delta n + 2n)$. After a 1st order Taylor approximation of $(1 - r_d)^2$ around $\Delta n = 0$, we find $\Delta I(b)/\Delta I_i(b) \approx 1 - \Delta n(b)/n(b)$.

In total, there is a direct relationship between the intensity change $\Delta \Phi = \Delta I_i(b) - \Delta I(b)$ in the bright field image on the CCD, the gradient of refractive index $\Delta n(b)$, and optical gradient force $F_{grad}(b)$ according to eqn (3):

$$\Delta I(b) \propto \Delta n(b) \propto F_{grad}(b)$$

Fig. 2 illustrates the implications, which can be made for all four cell types. If a cell shall be moved along the yellow-dashed line, the magnitude of the optical forces can be expected to be highest where $\Delta \Phi$ has a minimum. This is exactly the location where the sorter can grab a cell, independently of its actual size or shape.

![Fig. 2](image-url)
Fig. 3a illustrates how the relation in eqn (6) can be used to determine the 2D coordinates of a trap path for sorting in the x-direction. First, the minimum of ∆x in the x-direction (search starts at cell centre) is localized. This point, where highest trapping forces are expected, is defined as xcell. If cells have different sizes or if they enter the channel slightly out of focus, the precision of finding xcell can vary and so there is a risk of missing some cells. In order to trap every cell with a high reliability, it is beneficial to sacrifice a bit of displacement time and place the trap initially at a small distance x0 closer to the cell centre (x0 = 15% of distance between xcell and cell centre). Starting from this initial position x0 (see Fig. 3a), the trap moves with a velocity vtrap(t = 0) = vmin in the x-direction. It accelerates constantly over a distance xa, until it reaches its maximum velocity vmin. On the remaining and major part of the trap path, the trap moves with vmin. The idea behind this velocity profile is that trap and cell can find their optimal position relative to each other (xtrap(t > xa) = xcell(t > xa)). The farther the trap has moved from x0 towards xcell, the more likely it is that the trapping force Fgrad has reached its maximum and exceeds the viscous drag force Fv = 6πRgυxcell (R = cell radius, ς = viscosity of fluid medium). In the y-direction, the trap moves constantly with the velocity of the fluid to avoid additional viscous drag forces. Since all cells flow in the same height directly above the bottom of the fluid chamber, the optimal z-position between chamber, cells and trap can be achieved by simply focusing the cells in the focal plane, which is the trap’s z-position.

When a cell is released after the velocity dependent displacement time τ(vmax) = (2x0)/(vmin − vmin) + (d − x0)/vmx, its centre has moved in total a distance xcell(τ) = ∆xcell in sorting direction (Fig. 3b). To allow undisturbed displacement and regular transport of cells, the suspension is enclosed by sheath flows containing buffer medium. Image processing consumes computing power and thus is restricted to an area marked with the larger red-dashed rectangle. Once a cell is classified as positive within the small red rectangle (sorting region), it is sorted according to the described trap path. Cell positions can be recorded immediately before and after dragging.

**Software**

The operating software is written in Python using SciPy/NumPy modules for calculations and image processing. Image analysis consists of the following steps: (1) subtraction of background, (2) thresholding, (3) binary dilation, (4) fill holes, (5) binary erosion, and (6) labelling of all remaining objects. Image processing takes about 15 ms per frame on a 3 GHz CPU (Intel, Core 2 Duo). Classification and localization of cell centres and trapping positions depend on the number of labelled particles and consume around 6 ms. Coordinates of the best trap path are usually calculated in less than 1 ms.

**Results and discussion**

**Determination of displacement efficiency for different cell types**

Although the sorter can handle a broad variety of cells in a flexible way, it is important to know how fast different types of cells can be moved (vmax) or how short displacement times τ can be. In order to address this question in an automated and reproducible way, the flow of the medium and the cells in the microchannel was generated by moving a piezo stage (MCL, Nano-View) back and forth with a random displacement in the orthogonal direction. As classification requirements, cells had only to be within a certain size range in the bright field image.

As an invariable sorting condition, a nominal displacement distance of d = 40 μm and an acceleration distance of xa = 8 μm were chosen, comparable to the situation in the microchannel. Thereby, one can define a displacement efficiency η(τ) = Δxcell(τ)/d, where Δxcell is the actual displacement. One can expect

$$\eta(\tau) = \begin{cases} 1 & \text{if } F_{grad}(\tau) = 1 \\ 0 & \text{if } F_{grad}(\tau) < 1 \end{cases}$$

which means that the sorting efficiency should drop down rapidly as soon as Fv exceeds Fgrad. η can be increased with stronger optical forces Fgrad and with smaller cell radii R.

As illustrated in the example of a yeast cell in Fig. 4a, cells were moved in flow direction (y-direction) by the piezo stage with a velocity of vflow = 80 μm s⁻¹. Once they entered the sorting region, they were immediately displaced, released, and further transported in flow direction by the medium. For the next cycle, flow and sorting direction were flipped and the x-position of the cell was changed by a random value Δx between −5 μm and +5 μm since the cell’s x-position in the microchannel also varies within a similar range. The trap velocities vmin and vmax were increased after 10 cycles, such that after 200 cycles 20 different velocity pairs were applied. Immediately before and after sorting of each cycle, cell positions (centre-of-mass) were recorded, as well as the displacement distance Δxcell and the displacement time τ. These records are plotted in Fig. 4b for the case of Bacillus subtilis. As the maximum trap speed vmax increases, τ decreases. At the beginning, the measured displacement distance in x-direction Δx is close to d, but with increasing speeds and rates 1/τ the displacement Δx drops off abruptly and significantly, since $F_{grad} < 6πRgυx/Dτ$. We did not evaluate cycles, where a cell was dragged out of the trap due to too high trap velocities ν in a previous cycle, i.e. when $ν × τ = Δx < 0.9 × 40$ μm.
It can be observed that there are two reasons for the efficiency to drop below $\eta = 1$. In cycles marked with A, the cell dropped out of the trap during acceleration exactly when the viscous drag force $F_c$ becomes higher than the optical trapping force $F_{\text{grad}}$. In cycles marked with B, however, cell and optical trap cannot find their optimal position relative to each other and thus the cell is not displaced at all. These errors can in principle be eliminated by giving the image processing algorithm more real-time properties, which improves the estimate of how far a cell will have moved along $y$ until the optical trap becomes active. These sorting errors due to missing a cell’s cross-section only occur for very small cells.

In Fig. 4c, the displacement efficiencies $\eta(t) = \Delta x_{\text{cell}}(t)/d$ for protoplasts, mitochondria, yeast cells, and rod-shaped Bacillus subtilis are plotted. Sigmoidal fits illustrate the drop in sorting probabilities for critical displacement rates $1/\tau_{\text{crit}}$ for each cell type. All efficiencies with the same parameters are averaged and marked as dots. At the lower end of displacement rates, we find the protoplast, which is largest in radius ($2R \approx 20–30 \mu m$) and thus has the highest hydrodynamic resistance $F_c$. On the other end, the rod-shaped bacillus orients vertically inside the axial extended trap and thus maximizes the overall polarisability $\alpha$, while experiencing modest friction forces due to a cross-section of $1 \mu m \times 4 \mu m$. In addition, it has a cell wall with a higher refractive index and higher structural $\alpha$ than the mitochondrion, which is only enclosed by a membrane. (Videos can be found as ESI S1–S4.)

Fig. 4d gives a qualitative explanation for the drop of efficiency (region A in Fig. 4b). The efficiency $\eta(t)$ is time dependent since both the optical gradient force $F_{\text{grad}}$ and the viscous drag force $F_c$ increase with displacement time $t$. $F_{\text{grad}}$ changes qualitatively according to $-d/dt b(t) \exp(-b^2/\sigma^2)$ with the particle displacement $b(t)$, which itself increases with time. $F_c$ increases with the particle velocity $v(t)$, which also increases with time. As soon as the maximum optical force is reached, the particle drops out of the trap and the ratio of both forces drops abruptly. It is worth noticing that sorting can also work with efficiency below 1.0, since the optical trap can grab the same cell.

**Fig. 4** Displacement of different cells out of a flow. (a) Flow in a microchannel is emulated with a moving piezo stage at $v_{\text{flow}} = 80 \mu m s^{-1}$. Cells can be repeatedly and automatically displaced with the optical trap by reversion of the sorting direction after each “flow-through”. 2 cycles through the sorting region are marked with yellow dashed lines. $\delta x$ indicates the flow position uncertainty along $x$, $d$ is the nominal displacement. (b) The measured displacement duration $\tau$ (red), the nominal displacement distance $d$ (green), and the actual displacement distance (blue) are recorded as a function of maximum trap speed $v_{\text{max}}$. (c) The displacement efficiency $\eta$ as a function of displacement time $\tau$ for all four cell types. Efficiency drops abruptly for a critical displacement time $\tau_{\text{crit}}$. Possible sorting rates $1/\tau_{\text{crit}}$ are given for $\eta = 0.9$. (solid markers). The solid lines represent sigmoidal fits to estimate the probabilities of correct sorting. (d) Qualitative change of optical force $F_{\text{grad}}$ and viscous drag force $F_c$ over time for the case that a cell drops out of the trap during acceleration. At $\tau_{\text{crit}}$, the optical force can no longer counteract the viscous drag force and efficiency drops to zero.
Fig. 5 (a) Sorting of yeast cells in a microfluidic chamber by fluorescence level and size. Cells are classified by a fluorescence image (see green spots in the excitation region) and are localized in the subsequent bright field image. Positively classified cells are sorted to the upper outlet. Inlet images (16 μm × 16 μm) give an impression of resolvable features for classification. In the image sequence (b), fluorescent cells (A, B) are sorted out, non-fluorescent ones (C) not. In sequence (c), the fluorescent cell D is sorted, while structure E is a small fluorescent particle and consequently ignored. The time difference between the left and the right frame of the sequences (b) and (c) is 0.34 s. (Video available online as ESI S5.)

Conclusions

We have presented an active optical cell sorter based on fast steerable optical tweezers. By self-optimization of the acting optical gradient force versus the drag force, the system is able to sort a variety of cells having different shapes and sizes. No intermediate calibration is necessary. We have derived how the optimal trapping force within a cell can be found from the bright field image of the cell. Currently, the sorter’s through-put is limited to about 1 Hz. However, because of the high speed and reliability of the cell displacement by the trap, short sorting time periods τ could be identified. The measured τ ≈ 20 ms for Bacillus subtilis, 25 ms for yeast cells, 30 ms for 2 μm small mitochondria and 90 ms for large plant protoplasts could in principle result in sorting rates of 10–50 Hz. In particular, we were limited by the camera and the image processing, which can be sped up further by reducing the area of interest to the sorting region or using a faster and better camera than the simple CCD used in our approach. The key challenge is to adjust the microfluidic system in a way that cells enter the sorting region in a dense chain, without sticking together.

Sorting of yeast cells in a microfluidic chamber resulted in a recovery rate of 95% at a throughput of 1.4 cells s⁻¹. The recovery rate is defined as the fraction of those positively classified cells which reach the channel for sorted cells. 89% of the cells found in this channel were confirmed to be positive after sorting (11% false positive). This purity was only slightly lower than in a previously reported work, but still very satisfying, since classification criteria were more challenging and neither the microfluidics nor the laser power was optimised for this type of cell. The purity will be further increased if those cells that stick
together are ignored. Cell clusters were not treated differently during image processing. By doing so, either the number of false positive or false negative cells will be minimized.

A significant advantage of the system is the low degree of stress induced to cells. Previous works have shown that the risk of photo-damage due to the trapping laser light is very low, e.g. yeast cells can bear 180 mW of laser power over 50 s. In our case the sorting time is less than 100 ms and therefore the potential photo-toxicity can be clearly neglected. For yeast, damage resulting from the microfluidic system and fluorescence potential photo-toxicity can be clearly neglected. For yeast, case the sorting time is less than 100 ms and therefore the sophisticated morphological properties, which may not only check for the size of a cell, but for more well sortable with optical tweezers.

Moreover, protoplasts are very fragile and cannot be sorted in a FACS machine because of too strong accelerations, but are well sortable with optical tweezers.

More complex classification algorithms could easily be added, which may not only check for the size of a cell, but for more sophisticated morphological properties, e.g. if the nucleus is fluorescing and the cell is elongated, indicating an on-going cell division.

These advantages make an optical tweezers-based cell sorter with self-optimised trap dynamics a top candidate for sorting of small cell populations encoded with the most manifold features and characteristics.

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