Article

Measuring Local Viscosities near Plasma Membranes of Living Cells with Photonic Force Microscopy

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ABSTRACT The molecular processes of particle binding and endocytosis are influenced by the locally changing mobility of the particle nearby the plasma membrane of a living cell. However, it is unclear how the particle’s hydrodynamic drag and momentum vary locally and how they are mechanically transferred to the cell. We have measured the thermal fluctuations of a 1 μm-sized polystyrene sphere, which was placed in defined distances to plasma membranes of various cell types by using an optical trap and fast three-dimensional (3D) interferometric particle tracking. From the particle position fluctuations on a 30 μs timescale, we determined the distance-dependent change of the viscous drag in directions perpendicular and parallel to the cell membrane. Measurements on macrophages, adenocarcinoma cells, and epithelial cells revealed a significantly longer hydrodynamic coupling length of the particle to the membrane than those measured at giant unilamellar vesicles (GUVs) or a plane glass interface. In contrast to GUVs, there is also a strong increase in friction and in mean first passage time normal to the cell membrane. This hydrodynamic coupling transfers a different amount of momentum to the interior of living cells and might serve as an ultra-soft stimulus triggering further reactions.

INTRODUCTION

A biological cell can be considered as a minimal living system to respond to external disturbances. Among the many different kinds of stimuli that a cell is exposed to, mechanical contacts at the cell surface play a superordinate role (1,2), because cells are in constant mechanical interaction with their environment. The question of how a cell reacts to an approaching particle is of principal interest for various disciplines ranging from immunology (3,4) to drug delivery (5–7), and it is connected to the preceding question of how much time is given to a cell to react adequately to an approaching disturbance such as a bacterium, a virus, a vesicle, or inorganic particles delivered deliberately or unintentionally from outside.

The characteristic reaction time of a cell can be defined by a time period that starts with a stimulus of transmembrane receptors or of molecules in the pericellular/extracellular matrix (8), which can be measured by, e.g., small changes in the fluctuation amplitude of the approaching particle (9). The end of the reaction time can be defined by a measurable reorganization of membrane proteins or cytoskeleton proteins. This reaction can be further amplified by the duration and the amplitude of the stimulus, e.g., the ongoing approach of the particle. During the stimulus, the particle typically diffuses passively nearby the cell membrane on a timescale that is dominated by the viscosity of the extracellular fluid. Generally, the equilibrium association constant for two binding partners does not depend on the viscosity—provided reaction time is not limited. However, an increase of the viscosity η nearby the cell membrane is accompanied by a decrease of the collision rate fc ~1/η with the cell membrane and thus by decreased binding and reaction probability (10,11). The variation in the viscous drag γ ~ η of the approaching particle regulates the transfer of hydrodynamic momentum to the cell and thereby the amplitude of a stimulus and eventually of the cellular response. In this study we investigate the distance-dependent behavior of the mobility μ = 1/γ near the membranes of living cells, which has been measured so far only in specific viscoelastic relaxation experiments (8).

The change of the viscosity experienced by a particle near a stiff plane interface, i.e., its hydrodynamic coupling to the wall, has been put on a solid theoretical basis by the 1963 work of Happel and Brenner (12), who were able to predict the increase of a particle’s viscous drag parallel and perpendicular to the interface as a function of the separation distance. Theoretical studies by Lee (13,14) and Bickel (15,16) showed that the increase in static viscous drag at a fluid interface is very similar to that of a stiff interface in perpendicular direction, but is hardly visible parallel to the fluid interface. The theoretical work of Bickel (15) was extended to deformable membrane interfaces, considering different spatial and temporal frequencies at the deforming membrane (16).
A variety of experimental efforts were undertaken to confirm the theoretical predictions of the space variant viscous drag or diffusion constants of microbeads at stiff planar interfaces and alterations thereof. This was either realized by video tracking of a diffusing particle (17), by evanescent wave scattering (18–20), by analyzing the bead fluctuations inside an optical trap (21,22) or attached to the cantilever of an atomic force microscopy (23), or by using fluorescence correlation spectroscopy of fluorescent beads (24). In this context, optical traps enabled the measurement of the Derjaguin-Landau-Verwey-Overbeek potential in combination with viscous relaxation experiments near the interface (25). Instead of mapping the position-dependent local diffusion normal to the interface, Pralle et al. (26) succeeded in mapping the changes in lateral diffusion inside plasma membranes revealing sphingolipid-cholesterol rafts.

More complex situations of hydrodynamic coupling lengths and temporal mode relaxation of several particles were investigated by either time multiplexed point traps (27–29), holographic optical traps (30,31), and optical line traps, enabling direct contact between the particles (32–34).

The most elegant way to measure local diffusion coefficients or viscous drags is to analyze the thermal position fluctuations of trapped particles. Whereas the analysis of fluctuation amplitudes provides information about the trapping potential and the local environment (35), the analysis of the position autocorrelation (AC) functions or the power spectral density (PSD) also enables the extraction of the viscous drag of the particle’s motion (36). On very short timescales, this enables a three-dimensional (3D) viscosity mapping of small volume elements on the length scale of 10 to 30 nm (37).

Although the combination of optical traps and fast 3D position particle tracking, preferably by using back focal plane (BFP) interferometry, is quite established, no experiments have been performed to measure the distance-dependent change of the viscous drag near the plasma membrane of a living cell.

In this study, we investigate the change of the viscous drag close to the plasma membrane for three different types of mammalian cells and giant unilamellar vesicles (GUVs) (38). We analyze the 3D position fluctuations on a μs timescale to extract the viscous drag at the position of the diffusing particle, which is controlled by an optical trap. We show that the hydrodynamic coupling lengths normal to the cell membrane can be measured with good reproducibility, and demonstrate that this length can vary significantly for different cell types.

**Theoretical background**

**Thermal position fluctuations**

The bead’s stochastic motion in the presence of linear external forces can be theoretically described by a Langevin equation (39). In our case, it can be well approximated by the following:

\[
\dddot{\mathbf{r}}(t) + \mathbf{b} + \left( \mathbf{k}_\text{opt} - \mathbf{k}_\text{cel}(d) \right) = \mathbf{F}(t),
\]

where the position vector \( \mathbf{b}(t) \) denotes the bead’s displacement with respect to the trap center at a given time \( t \), and \( d \) is the distance of the cell membrane to the center of the laser focus; see Fig. 1 B. The trap center is ~0.2 μm behind the laser focus because of the radiation pressure (9). As the condition for overdamped motion for a high-enough viscous drag \( \gamma \) (i.e., \( \gamma^2 > 4 mk_b T \)) is fulfilled, the inertia term \( m \cdot \mathbf{b} \) was neglected. The spherical particle is driven by an uncorrelated random thermal force \( \mathbf{F}_\text{th}(t) \) with \( \langle \mathbf{F}_{\text{th},j}(t) \times \mathbf{F}_{\text{th},j}(t + \tau) \rangle = 2 \gamma_{j} k_b T \delta(\tau) \), which accounts for the Brownian motion of the particle with thermal energy \( k_b T \). Choosing the cell surface normal to one coordinate axis, \( \gamma \) is approximately a diagonal tensor with diagonal elements \( \gamma_{j} \), being the viscous drag coefficients for each spatial dimension \( j = x,y,z \). As all nondiagonal matrix elements \( \gamma_{ij}(d) = 0 \) vanish, we can refer to the diagonal elements as \( \gamma_{j}(d) \) instead of \( \gamma_{ij}(d) \). In general, \( \gamma_{j}(d) \) varies with the distance \( d \) to an obstacle, which in our case is the membrane of a living cell. To fit the data presented in the results section, we assume the diagonal drag coefficients \( \gamma_{j} \) to have the following form:

\[
\gamma_{j}(d) \approx \gamma_0 \times \exp\left( - \frac{(d - R)}{\Lambda_j} \right) + \gamma_{\infty},
\]

**FIGURE 1** Sketch of the experimental setup. (A) A 1 μm polystyrene bead is fluctuating in the proximity of a living cell. An optical trap confines the motion of the particle to a small volume around the trap center with FWHM = 18 nm in \( x \) and \( y \), and FWHM = 40 nm in \( z \) direction. The trap is moved toward the cell membrane with \( \Delta z = 20 \) nm steps by means of a 3D piezo stage. The bead’s fluctuation data are recorded in three dimensions (lower right) with 2 MHz temporal resolution via two QPDs. For simplicity, only one QPD is drawn in this setup sketch. (B) The distance between the center of the optical trap and the cell membrane is denoted as \( d \), whereas \( \mathbf{b} \) symbolizes the bead’s displacement from the trap center. The blue halo surrounding the cell membrane indicates the spatially varying viscous drag \( \gamma(d) \). To see this figure in color, go online.
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and small displacements, which is a valid assumption in all our experiments. Upon binding to a cell, an additional, a priori unknown stiffness parameter \( \kappa_{\text{cell}} = (\kappa_{\text{cell,ij}} \times \delta_{ij}) \) contributes to the bead’s motion. \( \kappa_{\text{cell}} \) can be approximated by a step-function, which is zero for distances \( d > R \) to the membrane, such that the total force constant experienced by the particle in direction \( j \) is \( \kappa_j(d) = \kappa_{\text{cell,ij}}(d) + \kappa_{\text{opt,ij}} \) such that \( \kappa_j(d > R) = \kappa_{\text{opt,ij}} \). Because both the optical force \( \kappa_{\text{opt}} \times \mathbf{b} \) and the friction force \( \gamma_j(d) \times \mathbf{b} \) point in the opposite direction of \( \mathbf{b} \) and \( \mathbf{b} \), respectively, they have the same sign. However, the force exerted by the cell, \( -\kappa_{\text{cell}} \times \mathbf{b} \), which only applies when \( d < R \), tends to push the particle out of the trap, i.e., acts in the opposite direction and therefore has a negative sign.

A suitable and common method to determine the quantities \( \kappa \) and \( \gamma \) from the fluctuation data is correlation analysis (39). Assuming a linear force and friction acting on the particle in thermal equilibrium, the autocorrelation function for the particle’s position is given by the following:

\[
\begin{align*}
AC(b_j(t)) &= \langle b_j(t) \times b_j(t + \tau) \rangle = \langle b_j(0)^2 \rangle \times e^{-\tau/\tau_0} \\
&= \frac{k_B T}{\kappa_j(d)} \times \exp(-\tau \times \kappa_j(d)/\gamma_j(d)).
\end{align*}
\]

(3)

For time delays \( \tau \) much shorter than the AC time \( \tau_0 = \gamma_j/\kappa_j \), \( AC(b_j(t)) = AC_j(\tau) \) is approximately linear, resulting in the following:

\[
AC_j(\tau \ll \tau_0) \approx \frac{k_B T}{\kappa_j(d)} \left( 1 - \tau \times \kappa_j(d)/\gamma_j(d) \right) = \frac{k_B T}{\kappa_j(d)} - \frac{k_B T}{\gamma_j(d)} \times \tau.
\]

(4)

The static part (\( \tau = 0 \)) of the AC yields the stiffness parameter \( \kappa \). The dynamical information extracted from the slope \( k_B T/\gamma_j(d) \) of the AC for short time delays \( \tau \) yields the friction coefficient \( \gamma \).

Mean first passage time

The average time a particle needs to diffuse over a given distance is defined as the mean first passage time (MFPT). Often, diffusion of a particle over its own radius \( R \) is considered. In the absence of interfaces or for distances large enough that no disturbance of the diffusive motion occurs, i.e., \( d - R \gg A_j \), the MFPT simply reads \( \tau_0 = (R^2/2k_B T) \times \gamma \), which can be derived from the particle’s mean squared displacement (39). If hydrodynamic coupling to the interface has to be considered, i.e., for \( d - R = A_j \), the spatial variation of the viscous drag has to be taken into account. For our exponential approach in Eq. 2, the following is the modified formula for the MFPT \( \tau(d_1, d_2) \):

\[
\begin{align*}
\tau(d_1, d_2) &= \frac{R^2}{2k_B T} \times \left( \frac{1}{d_2 - d_1} \int_{d_1}^{d_2} \gamma + \gamma_0 e^{-(d-R)/A_j} \, dd \right),
\end{align*}
\]

(5)

where the multiplication with a constant factor \( \gamma_0 \) has been replaced by an integral accounting for the distance-dependent change of \( \gamma_j(d) \), normalized by the prefactor \( (d_2-d_1) \), and \( d_1 \) and \( d_2 \) are the boundaries confining the diffusion area in perpendicular direction.

Interferometric particle tracking and signal acquisition

The determination of the particle’s displacement \( \mathbf{b}(t) \) in our situation is not straightforward. The tracking scheme is based on intensities \( I_{\text{tot,2}} = |\mathbf{E} + \mathbf{E}_p|^2 \) generated by the interference of the electric field of the unscattered trapping light and the light scattered at the particle, \( \mathbf{E} \) and \( \mathbf{E}_p \). These intensities in the BFP are recorded by one or two quadrant photo diodes (QPDs); see Fig. 1. A QPD measures four voltage signals, each proportional to the interference intensity \( I_{\text{tot}} \), which is integrated over the area of each quadrant. The voltage signals are then combined to result in three position signals \( S_j(t) \) that are functions of the particle position \( b_j(t) \). \( S_i \) is obtained from the difference of the two left and the two right quadrant signals, and \( S_i \) from the difference between the upper and lower two quadrant signals. The axial position signal \( S_0 \) is provided by the sum of all four QPD signals and varies linearly with small axial displacements \( b_z \) of the particle. Therefore, the position signal recorded in the BFP of the detection objective lens (Fourier plane) with coordinates \( (k_x, k_y) \) can be described as \( S_j(k_x, k_y) \), \( j = 1, 2 \), \( H_j(k_x, k_y) \) \( dk_xdk_y \) (40). The vector function \( \mathbf{H} \) is a filter selecting the three directions \( j = x, y, z \) out of the interference pattern \( I_{\text{tot,2}} \) through \( \mathbf{H}(k_x, k_y) = \text{step}(k_0 N_{\text{det}} - |k|) \times (2 \text{step}(k_x) - 1, 2 \text{step}(k_y) - 1, 1) \). \( k_0 = 2\pi/\lambda \) is the vacuum wavelength of the trapping light with wavelength \( \lambda = 1.06 \mu m \) and \( N_{\text{det}} \) is the numerical aperture of the detection lens. Within the small spatial displacements \( b_j \) occurring in all our experiments, the signals \( S_j \) are proportional to the actual displacements. The conversion factor is the detector sensitivity \( g_j \) and is given by \( S(t) = g_j \times b(t) \). Before each experiment, i.e., in the absence of the cell, the undisturbed detector sensitivities \( g_{\text{cell}} \) are determined by the Langevin calibration procedure (41).

If a particle diffuses nearby the cell, the incident trapping light can be scattered at the periphery of the cell as well, such that three beams with electric fields \( \mathbf{E}_i, \mathbf{E}_p, \) and \( \mathbf{E}_c \) \( (i = \text{incident}, p = \text{particle}, c = \text{cell}) \) can interfere. The three-beam interference generates an intensity pattern \( I_{\text{tot}}(k_x, k_y) \) in the BFP of the detection objective lens (Fourier
plane) with coordinates \((k_x, k_y)\) \((40)\), which is imaged onto the QPD and can be described by \((42)\) the following:

\[
I_{\text{tot},3}(b, d) = \left| E_i + E_p(b) + E_c(d) \right|^2 = \left| E_i \right|^2 + \left| E_p \right|^2 + \left| E_c \right|^2 + 2\left| E_i \right| \left| E_p \right| \cos(\phi_i - \phi_p(b)) + 2\left| E_i \right| \left| E_c \right| \cos(\phi_i - \phi_c(-d)) + 2\left| E_p \right| \left| E_c \right| \cos(\phi_p(b) - \phi_c(d)).
\]

\((6)\)

The three-beam interference consists of six terms, with three additional intensities generated by the distance-dependent electric field \(E_c(d)\) scattered at the cell periphery. For large distances \(d\), these terms vanish and the well-known two-beam interference formula is left over. Because the distance \(d\) is a positive number, we indicated the origin of the scattered phase \(\phi_c(-d)\) by a negative argument, because the cell is placed left to the optical axis and the particle is right to the optical axis. Equation \(6\) can be summarized to the incoherent parts \(I_i + I_p(b) + I_c(d)\), two terms with sine functions both defined by the interference of the incident field and a scattered field, which are phase shifted by \(\pi/2\), and, a cosine term defined by the interference between the two scattered fields, \(E_p\) and \(E_c\):

\[
I_{\text{tot},3}(k_x, k_y, b, d) \approx I_i + I_p(b) + I_p(b)\sin(\Delta \phi_p(b)) + I_c(d) - I_p(d)\sin(\Delta \phi_p(d)) + I_p(b, d)\cos(\Delta \phi_p(b, d)).
\]

\((7)\)

The second sine term does not change on timescales smaller than the measurement time, because it does not depend on the fluctuating particle position \(b(t)\). The cosine term, defined by both scattered fields, is small and can be neglected. According to Fig. 1 B, the cell is displaced in the one and the bead in the other direction relative to the center of the field’s focus with phase \(\phi_c\). In this way, the two sine functions in Eq. 7 have different signs, because the phase difference \(\Delta \phi_c(d) = \phi_1 - \phi_c(-d)\) is an odd function, i.e., \(\Delta \phi_c(d) = -\Delta \phi_c(-d)\). Thereby, the distance-dependent term \(I_c(d)\sin(\Delta \phi_c(d))\) flattens the total interference pattern across the QPD and reduces the mean value of the total signal \(S_j(b_j, d)\) according to the following:

\[
S_j(b_j, d) \approx \int \int_{QPD} I_{\text{tot},2}(b_j) H_j \, dk_x dk_y + \int \int_{QPD} (I_c(d) - I_p(d)\sin(\Delta \phi_p(d))) H_j \, dk_x dk_y = S_{ipj}(b_j) - S_{icj}(d).
\]

\((8)\)

For small displacements, the position signal \(S_{ipj}(b_j(t)) \approx S_0 + g_{ij} \times b_j(t)\) is a linear function of displacements \(b_j(t)\). According to Eq. 8, the distance-dependent signal \(S_{icj}(d)\) generated by the cell reduces the measured signal \(S_j(b_j, d)\) with decreasing distance \(d\), but does not depend on the particle displacements \(b_j\) and thereby on the fluctuation width \((b_j(0))\). As shown by the green trajectory in Fig. 3 A, the vicinity of the cell will affect the mean signal offset, leading to an apparent particle displacement perpendicular to the cell surface, which is merely an optical effect. However, the amplitude of the position fluctuations \((b_j(0))\) is hardly affected.

Following Eq. 8, the AC of the particle’s position signal is the sum of a time-varying and a temporally constant function, \(AC(S(b(t), d)) = AC(S_{ipj}(b(t)) - S_{icj}(d))\) and can be written as the sum of two AC functions: \(AC(S(b(t), d)) = AC(S_{ipj}(b(t))) + AC(S_{icj}(d)) - 2 \times CC(S_{ipj}(b(t)), S_{icj}(d)).\) The cross correlation between the conventional fluctuation signal and the DC signal from the cell is zero. The first AC function is the exponential of Eq. 3, the second is a wedge function characterized by the time-constant signal amplitude \(S_{icj}(d)\).

\[
AC(S_j(b_j, d)) = g_j \frac{k_BT}{k_j} \times \exp\left(-\frac{\tau \phi_j}{\gamma_j(d)}\right) + S_{icj}(d) \left(1 - \frac{\tau}{\tau_{\text{mes}}}\right) \quad (9)
\]

\[
\tau_{\text{mes}} < \tau_0 = g^2 \left(\frac{k_BT}{k_j} - \frac{k_BT}{\gamma_j(d)} \cdot \tau\right) + S_{icj}(d)^2.
\]

\(A\)

J774

HT29

MDCK

\(B\)

FIGURE 2 Three-dimensional configuration of the cell membrane interface. (A) DIC images of different cell types with a 1 µm diameter polystyrene bead. From left to right: J774 macrophage, HT29 adenocarcinoma cell, and MDCK epithelial cell. (B) Three-dimensional cell image of a HT29 cell, reconstructed from x-y-slices taken at different z-positions, which are \(dz = 1 \mu m\) apart. The blue frame indicates the height above the cover slip at which the bead was placed. The additional slices illustrate the estimation of the cell’s radii of curvature (yellow frame: x-y-plane, orange and red lines: y-z-plane). To see this figure in color, go online.
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Carl Zeiss) is used to collect the unscattered laser light and the light scattered by the cell. The experimental setup is shown in Fig. 1.

A simplified sketch of the optical setup is depicted in Fig. 1. The laser power is stabilized by a noise eater (miniNE Opto-Electronique, Orsay, France) and controlled by a surrounding heating element (TC-CSC, Bioscience Tools, Germany). The temperature of the cell medium inside the sample chamber can be controlled by a proportional-integral-derivative controller (TC-2-100, Bioscience Tools, Germany).

Sample chamber with heating unit

The temperature of the cell medium inside the sample chamber can be controlled by a surrounding heating element (TC-CSC, Bioscience Tools, San Diego, CA), which has an integrated temperature sensor and is regulated via a proportional-integral-derivative controller (TC-2-100, Bioscience Tools). The heating unit is switched on ~1 h before the experiments.

However, on short timescales \( \tau < \tau_0 \), \( \tau < \tau_m \), the additional signal \( S_d(d) \) generated by the cell does not affect the slope \( k_B T / \gamma / d \) of the AC function and thereby the viscosity \( \gamma / d \). Here, the measurement time at each trap position, \( \tau_m = 150 \text{ ms} \), equals ~100 times the AC time \( \tau_0 \).

### MATERIALS AND METHODS

#### Optical microscope

An inverted microscope (Axio Observer, Carl Zeiss, Jena, Germany) equipped with a high NA water immersion objective lens (C-Apochromat 63×/1.20W Corr M27, Carl Zeiss) was used for differential interference contrast (DIC) and bright-field microscopy. The DIC images were acquired by a 12-bit monochrome charge-coupled device camera (AxioCam MRm, Carl Zeiss).

#### Photonic force microscope

In brief, the photonic force microscope consists of an optical trapping unit and an interferometric tracking unit. The optical trap is formed by a 2 W Nd:GdVO₄ solid-state laser (Smart Laser Systems, Berlin, Germany) operating at 1064 nm in cw mode, which is focused onto the sample via the objective lens. An acousto-optical modulator (AA.MT.110/A1-ir, AA Opto-Electronique, Orsay, France) allowed for the control of the laser power in the focus. The laser power is stabilized by a noise eater (miniNE 2.1, TEM Messtechnik, Hanover, Germany), which analyzes the laser intensity fluctuations by a reference photo diode (G8370-81, InGaAs photo diode, Hamamatsu, Japan) and controls the transmission of the acousto-optic modulator via an external regulation circuit. A simplified sketch of the experimental setup is shown in Fig. 1.

#### Tracking unit

A second high NA objective lens (W Plan-Apochromat 63×/NAₐₙₙ = 1.0, Carl Zeiss) is used to collect the unscattered laser light and the light scattered at the bead and the cell periphery, respectively. The resulting interference patterns in the BFP are imaged onto two QPDs (InGaAs PIN photodiodes, G6849 series, Hamamatsu). The beam is split up by 50% beam splitter cubes after passing the detection objective and is imaged onto the QPDs with different magnifications, accounting for the different detection sensitivities for axial and lateral signals, respectively (43–45). The use of InGaAs photodiodes enables high-speed tracking with good quantum efficiency at 1064 nm. Incoming voltage signals are amplified by two miniSupply QUAD pre-amplifiers (TEM Messtechnik) and digitalized via two analog-digital converter cards (NIDAQ PCI-6110 and PCIe-6259, National Instruments, Austin, TX).

#### Cell preparation

For our cell experiments, we used J774 mouse macrophages (American Type Culture Collection ATCC, Manassas, VA) as an example for cells that exhibit phagocytic activity as well as HT29 human colorectal adenocarcinoma cells and Madin-Darby canine kidney (MDCK) epithelial cells, the latter two showing no phagocytic activity. The cells, shown in Fig. 2, were cultured at 37°C during all the experiments.

The three-dimensional QPD data are divided into \( d_{ starts with a \( y_{ end with a \( d_{ starts with a \( y_{ end with a \( d_{j} \text{ (red dot)} \) and \( y_{j} \text{ (green dot)} \) for the bead and the cell periphery, respectively. The parts of the trajectory that correspond to one specific cell-focus distance \( d \) are analyzed by means of AC functions. (D) The AC is approximately linear on a \( \tau \leq 30 \text{ μs} \) timescale, which is used to obtain \( /d \) and \( /d \). To see this figure in color, go online.
to allow the system to equilibrate, thus reducing thermal drifts during measurement. The sample chamber is connected to 3D piezo stage (NanoView LP200, Mad City Labs, Madison, WI) that provides a 200 μm range of motion with a step response of 20 ms for each dimension and with a positioning accuracy smaller than 1 nm. Moving the sample chamber relative to the static optical trap thus enables an accurate distance control.

RESULTS

Geometrical arrangement

The geometry of the interfaces is an important factor in all experiments. We have approximated the cell to be planar over the cross section of the bead. To back up this assumption, the cell’s radii of curvature were measured with the public domain software ImageJ (http://rsbweb.nih.gov/ij/) and compared with the bead’s radius. For the sample cell shown in Fig. 2 B, the radius of curvature in the x-y-plane of ~9.5 μm is 19 times larger than the bead radius \( R_{\text{bead}} = 0.5 \) μm, so that \( R_{\text{cell}} \gg R_{\text{bead}} \) is a valid assumption. All other cells used were of comparable size. In fact, the curvature of the cell has only a minor effect of \(<2.5%\) on the measured viscous drag \( \gamma(d) \) that can be estimated by some geometrical considerations (see Figs. S1 and S2 in the Supporting Material).

The \( z \)-distance of the bead to the cover slip was chosen high enough, i.e., at least five times the bead diameter, where the hydrodynamic effects are low, such that no interaction between bead and cover slip could deteriorate our measurements. The direction of light propagation is always denoted as \( z \), whereas the in-plane coordinates \( x \) and \( y \) are chosen such that \( x \) always denotes the direction parallel to the interface and \( y \) corresponds to the scan direction, i.e., perpendicular to the interface; see also Fig. 1. In the analysis of the hydrodynamic decay lengths and MFPTs, we limit ourselves to \( x \) and \( y \) data, to which we refer as \( || \) and \( \perp \), respectively.

Measuring the position signals

QPD signals were recorded with a sampling rate of 2 MHz, from which the bead’s position trajectories \( b_x(t), b_y(t), b_z(t) \) were calculated as shown above; see Fig. 3 A. During data acquisition, the piezo stage holding the cell sample was moved in \( y \) direction with 20 nm steps, hereby subsequently reducing the distance \( d \) between the center of the laser focus and the cell membrane. At each step, 300,000 data points were recorded, corresponding to a measurement time \( \tau_{\text{mes}} = 150 \) ms per position. This equals ~100 times the AC time, which has been shown to be beneficial for the reliability of the AC analysis presented in Fig. 3, C and D. The complete trajectories \( b_x(t), b_y(t), b_z(t) \) were cut into single segments corresponding to one fixed piezo position and analyzed separately. Although the full range of data points up to \( d = 0 \) is shown in Fig. 3 A, only distances \( d \geq R \) are considered for data evaluation. For \( d < R \), bead and membrane are already in close contact, so that the fluctuation width of the bead is narrowed and causing the bead to be shifted out of the laser focus, which can be seen as a strong displacement of the trajectories in all spatial dimensions. A control experiment of an empty trap approaching a cell membrane is presented and discussed in the Supporting Material; see Fig. S3.

Estimating the contact between bead and membrane

From the fluctuation data in scan direction, i.e., \( y \) data, position histograms were determined and the distance-dependent standard deviation of the bead trace \( \sigma_y(d) \) was analyzed; see Fig. 3 B. A decay of \( \sigma_y(d = R) = 50% \times \sigma_y \) to half of its bulk value reveals the position \( d = R \), where the bead and a stiff interface are in mechanical contact (46). The rationale behind this choice is further explained in the Supporting Material, alongside data from Brownian dynamics simulations that back up this criterion; see Figs. S4–S7.

However, if the bead comes into contact with a soft interface, such as the pericellular matrix (PCM), the bead’s fluctuation width can decay to \( \sigma_y / 2 \) before contact with the cell membrane, which might be only reached at a minimal width of about \( \sigma_y(d = R) \approx \sigma_y / 3 = \sigma_{\text{min}} \). At this point, stiff membrane contact is very probable, as the bead starts to get pushed out of the optical trap by the cell and the QPD signals merely arise from laser light scattered at the cell. The true membrane contact point is likely located between these two estimates. More precise values for the membrane contact point cannot be specified, because a certain influence of the PCM on the measured signals remains. Analysis of all \( \sigma_y(d) \) curves from each cell experiment reveals that the latest membrane contact point at \( \sigma_{\text{min}} \) is in average 0.22 μm ± 0.09 μm behind the 50% \( \sigma_y \) estimate and differs slightly between different cell types (J774: 0.27 ± 0.09 μm, MDCK: 0.19 ± 0.07 μm, HT29: 0.21 ± 0.11 μm).

Force constants and distance-dependent viscosities

We can assume the system to be in thermal equilibrium as long as no contact between bead and membrane is established. Then, the fluctuation data can be analyzed by means of correlation analysis to obtain information about the force constants \( k_j \) and the friction coefficients \( \gamma_j \); see Eq. 4. Fig. 4 A shows the stiffness \( \kappa_j(d) \) for varying distance \( d \) between the center of the laser focus and the cell membrane. All its components \( k_j \) \((j = x,y,z)\) remain constant until mechanical contact between the bead and the cell membrane is established, as indicated by additional line fits. The values obtained from these fits \((k_x = 50.8 \text{ pN/μm}, k_y = 47.6 \text{ pN/μm}, k_z = 13.4 \text{ pN/μm})\) agree well with the trap stiffnesses obtained from a Langevin-calibration before the experiment (not shown).
At the same time, the friction coefficients \( \gamma_j(d) \) increase as the bead approaches the cell membrane, starting \( \sim 1 \mu m \) before contact. The increase of the friction component perpendicular to the cell membrane, i.e., \( \gamma_y(d) \) displayed in green, is significantly higher than \( \gamma_x(d) \) and \( \gamma_z(d) \) in parallel direction (red and blue circles). This phenomenon has also been observed qualitatively in experiments of a spherical bead approaching a stiff wall (22).

Influence of filopodial binding on the fluctuation data

Macrophages are components of the mammalian immune system and possess small cell protrusions called filopodia, which can act as tentacles to pull bound objects toward the cell to initiate a process called phagocytosis (47,48). The measurements performed with macrophages require special attention because of possible binding events to cellular protrusions such as filopodia. Binding to such protrusions would make it impossible to extract information about pure hydrodynamic coupling out of the fluctuation data. During all experiments with cells, care was taken to investigate only parts of the membrane where no protrusions could be observed in the DIC images. However, binding to tiny filopodia that are invisible in the microscope can still have an influence on the measurement data and must be disregarded, if any changes in the fluctuation width become visible in the particle tracking data before cell contact. Upon binding to the membrane, the particle fluctuation width reduces strongly and considerable forces would be required to detach the particle from the cell (49).

Fig. 5 illustrates how filopodial binding can be identified in the fluctuation data. First, the bead’s positions trajectories change slowly in their mean position values. Further analysis of the fluctuation behavior reveals that both \( \kappa_j(t) \) and \( \gamma_j(t) \) increase abruptly upon binding of a filopodium, while at the same time the fluctuation volume is restricted by the filopodium, resulting in a narrowed fluctuation width. The increase in \( \kappa_j(t) \) and \( \gamma_j(t) \) is most pronounced in the direction of filopodial retraction. As shown in Fig. 5, \( \kappa_x(t) \) and \( \kappa_y(t) \) increase rapidly to \( \sim 250\% \) of their original values. \( \gamma_x(t) \) and \( \gamma_y(t) \) increase even by a factor of 10. Note that this behavior is fundamentally different to the smooth increase shown in Fig. 4. In this way possible filopodial binding can be identified with the help of the fluctuation data. For all results shown in the following chapters, we could verify that no filopodial binding occurred.

The pericellular matrix of living cells

A large variety of eukaryotic cells including those examined in this study are known to have a structure that is covalently linked to the outer side of the plasma membrane, the so-called...
glycocalyx or PCM (8,49–51). It consists in particular of proteoglycans and associated polymer chains and is involved in plenty of cellular functions from cell adhesion and migration to receptor functions and immune response, only to mention a few. The thickness of the glycocalyx can exceed a few micrometers. As the PCM is invisible in brightfield or DIC microscopy, its occurrence is difficult to observe. However, its possible influence on the bead’s fluctuation upon cell approach must not be ignored. A discussion of possible effects will be provided later in the manuscript.

**Change of the local hydrodynamics close to a living cell**

The distance-dependent viscous drag close to an interface is displayed in Figs. 4 and 6. The exponential function given in Eq. 2 was fitted to the data points \( \gamma_j(d) \). The good fit results show that our exponential model is a suitable approach, which has the great advantage, that the hydrodynamic coupling of particles to the interface can be described by just two values for each direction, \( \gamma_{0j} \) and \( A_j \). The hydrodynamic decay length \( A_j \) is a measure for the distance, on which hydrodynamic coupling between the particle and cell increases the friction. In the limit \( d \to \infty \), i.e., far away from the cell, we measured a viscous drag \( \gamma_\infty = 8.0 \times 10^{-5} \text{Ns/m} \), which is the viscosity of the cell medium at \( T = 37^\circ\text{C} \) (52). \( \gamma_\infty + \gamma_{0j} \) is the maximum viscous drag that occurs when cell membrane and bead surface are in close contact.

Fig. 6 summarizes the fit results to the measured \( \gamma_j(d) \) curves for different cell samples using the contact point estimate at \( \sigma_0 \). In total, we investigated \( N = 16 \) J774 macrophages, \( N = 15 \) MDCK cells, \( N = 24 \) HT29 cells, and \( N = 11 \) GUVs. \( \gamma_\perp(d) \) reveals comparable slopes for all cell types, but does not increase as steeply as for the case of a stiff wall at small distances, i.e., \( 0.5 \mu \text{m} < d < 0.65 \mu \text{m} \). Although \( A_\perp \) is significantly higher than \( A_\parallel \) for all living cells, this is not the case for a GUV or a glass interface. The hydrodynamic decay lengths for perpendicular motion are approximately the same for the J774 (\( A_\perp = 0.49 \mu \text{m} \)) and the HT29 cells (\( A_\perp = 0.45 \mu \text{m} \)), whereas the decay length for the MDCK cells is ~30% longer (\( A_\perp = 0.65 \mu \text{m} \)). A similar result can be observed for the parallel decay lengths, which are generally 1.5 to 1.8 times smaller: J774: \( A_\parallel = 0.27 \mu \text{m} \), HT29: \( A_\parallel = 0.28 \mu \text{m} \), MDCK: \( A_\parallel = 0.34 \mu \text{m} \). The viscous drag increases with decreasing distance \( d \) between focus and interface and, within our measurement accuracy, reaches a finite value \( \gamma_j(d = R) = \gamma_{0j} + \gamma_\infty \); see Eq. 2 with \( j = \perp, \parallel \). The obtained \( \gamma_{0j} \) values are displayed in Fig. 6 C as a multiple of \( \gamma_\infty = 8.0 \times 10^{-9} \text{Ns/m} \). In the case of diffusion parallel to the interface, the viscous drag \( \gamma_{0j} \) is effectively the same for all cell types investigated and increases to roughly 280% of the bulk value. The perpendicular friction factor \( \gamma_{0\perp} \) is generally higher than \( \gamma_{0\parallel} \) and the values for different cell types differ by up to 20% from one another (HT29: \( \gamma_{0\perp} = 6.23 \times \gamma_\infty \), MDCK: \( \gamma_{0\perp} = 5.64 \times \gamma_\infty \), J774: \( \gamma_{0\perp} = 5.11 \times \gamma_\infty \)).

Using the \( \sigma_{\min} \) criterion for the contact point, the measured decay lengths \( A_j \) are slightly decreased (by maximally 12%) and the maximum friction coefficients \( \gamma_{0j} \) are increased by a factor of 1.39 to 2.31, depending on the cell type. A detailed comparison of all the results is given in the Supporting Material; see Tables S1–S3, together with a revision of Figs. 6, B and C, and 7 accounting for the uncertainty of the membrane position (see Figs. S8–S10).

The change in \( \gamma(d) \) of a bead approaching a plane stiff interface as a function of distance is well understood and can be theoretically calculated according to Happel’s and Brenner’s law (12). The corresponding measurement data is shown in the left inset of Fig. 6 A. The uncoated glass
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because of the scattering force.

has moved to the upper cover slip upon laser irradiation of the GUV membrane in perpendicular and parallel direction are about the same (\(\gamma_{\perp} = 1.10 \times \gamma_{\perp} = 1.08 \times \gamma_{\parallel} \)).

The fluctuation data from the GUV experiments and the extraction of \(\varepsilon_{d}(d)\) and \(\gamma_{f}(d)\) similar to the procedure shown in Fig. 4 is presented in the Supporting Material; see Fig. S13, together with Fig. S14 displaying the bead’s trajectory upon approaching the GUV membrane.

**Mean first passage times**

By means of Eq. 5, we analyzed the time a 1 \(\mu m\) bead needs to diffuse toward an interface from the distance \(d_{f} = 3R\) toward \(d_{f} = 2R\) with \(t_{0} = (R^{2}/2k_{B}T) \times \gamma_{\perp} = 0.234s\) for \(d-R >> A_{f}\) using the \(\sigma_{2}\) criterion for the contact point. As Fig. 7 shows, the increase in viscous drag near an interface causes the MFPTs to rise significantly. For living cells, an anisotropy of the MPFT is apparent. The diffusion perpendicular to the membrane is slowed down by a factor of up to 1.64 in the case of MDCK cells (J774: \(t_{\perp}(3R,2R) = 1.45 \times t_{0}\), HT29: \(t_{\perp}(3R,2R) = 1.39 \times t_{0}\)). In contrast, however, the MFPT for diffusion parallel to the interface is not affected severely, with a maximum increase of \(t_{\parallel}(3R,2R) = 1.18 \times t_{0}\) for the case of MDCK cells. The significantly increased \(t_{\perp}\) is unique to living cells and is not pronounced at the GUV membrane with \(t_{\perp}(3R,2R) = 1.08 \times t_{0}\) and \(t_{\perp}(3R,2R) = 1.06 \times t_{0}\). As the uncertainty in the determination of the true membrane contact point affects both \(A_{f}\) and \(\gamma_{\parallel}\), the \(t_{j}\) are also influenced. Using the \(\sigma_{min}\) contact estimate results in an overall increase of \(t_{j}\), which is again most pronounced in perpendicular direction.

Remarkably, and in contrast to the results for living cells, no significant difference in perpendicular and parallel hydrodynamic decay lengths (\(A_{\perp} = 0.28 \mu m, A_{\parallel} = 0.24 \mu m\)) could be observed; see Fig. 6 B. Both decay lengths are very similar to those \(A_{j}\) measured nearby living cells. The maximal friction close to the GUV membrane in perpendicular and parallel direction are about the same (\(\gamma_{\perp} = 1.10 \times \gamma_{\perp} = 1.08 \times \gamma_{\parallel} \)), again significantly different compared with the results of living cells.

The good agreement between our experimental data and the decay predicted by Happel and Brenner for the glass interface proves the validity of our measurement procedure. Applying our exponential decay model to the glass interface data yields decay lengths of \(A_{\perp} = 0.162 \mu m\) and \(A_{\parallel} = 0.157 \mu m\). These values do not exhibit a difference in both directions, but are significantly lower than those for living cells, i.e., about a factor of 3.5 for perpendicular and 1.9 for parallel motion. One should note that fitting the Happel and Brenner functions

\[
\gamma = \gamma_{\perp} \left(1-\frac{9}{16}R/d + \frac{1}{8}(R/d)^{3} \right) \quad (10)
\]

\[
\gamma = \gamma_{\parallel} \left(6(d-R)^{2} + 9 \times (d-R) \times R + 2R^{2} \right) \quad (11)
\]
to the \(\gamma(d)\) curves belonging to cell membranes or GUVs fails and that our exponential model shows more accurate fit results (not shown).

**Measurements on GUVs as artificial cells**

We have used GUVs as the simplest biomimetic model system for mammalian cells. As described in further detail by Meinel et al. (38), the GUVs were \(\sim 20 \mu m\) in diameter and were prepared from egg phosphatidylcholine (Egg PC, Sigma-Aldrich, St. Louis, MO), utilizing the method of electroformation. Different to the cells used, the GUVs are characterized by a lipid bilayer that separates two approximately identical fluids. Measurements on GUVs were performed with 1 \(\mu m\)–sized polystyrene beads and the same experimental parameters as described above, but with reduced laser power, resulting in slightly larger fluctuation volumes of the bead. The GUV was trapped in a sandwich configuration consisting of two uncoated glass cover slips separated by a 75 \(\mu m\)-thick spacer ring. Glass beads (\(2R = 20 \mu m\)) were attached to the downside of the upper cover slip to ensure the immobilization of the GUV, which has moved to the upper cover slip upon laser irradiation because of the scattering force.

![FIGURE 7 Anisotropic diffusion nearby interfaces. Mean first passage times \(t_{\perp}(d_{1},d_{2})\) and \(t_{\parallel}(d_{1},d_{2})\) for a 1 \(\mu m\) bead diffusing nearby an interface from \(d_{1} = 3R\) toward \(d_{2} = 2R\), as illustrated in the inset. Color coding is the same as in Fig. 6. To see this figure in color, go online.](image-url)
accounting for this contact point uncertainty are presented in the Supporting Material; see Table S3 and Fig. S10.

To calculate the MFPTs at the glass interface, we performed a numerical integration of Eq. 5, where the term \( \gamma_{\infty} + \gamma_0 e^{-(d-R)/A} \) was replaced by the respective approximation formula as given by Happel and Brenner (Eqs. 10 and 11). This analysis resulted in \( t_{g,Glass}(3R,2R) = 0.302 \text{s} \times t_0 \) and \( t_{g,Glass}(3R,2R) = 0.417 \text{s} \times 1.782 \times t_0 \). Those results are both even higher than those of all living cells, which is understandable, because the stiff character of the glass interface is expected to slow down the bead’s diffusion more drastically than the presence of a flexible plasma membrane.

### DISCUSSION

#### Short summary of the experimental results

In this study, we measured the diffusive behavior of 1 \( \mu \text{m} \)-sized particles in the vicinity of the plasma membranes of living cells, of a GUV, and a glass interface. We used a photonic force microscope equipped with a 3D interferometric tracking system, which allows us to record the Brownian motion of the particle at 2 MHz sampling rate and with nanometer precision. By analyzing the short timescale diffusion via the AC of the particle’s trajectory, we could observe and quantify a generally increased viscous drag near surfaces. For all cell types, the viscous drag perpendicular to the membrane is increased more significantly than in parallel direction. This behavior could not be observed for the GUV.

#### Accuracy of determining the bead-membrane-distance

Although the distance was reduced in steps of 20 nm, the relatively strong laser power restricted the bead diffusion to an area with radius of roughly 9 nm, both for parallel and perpendicular diffusion, which is less than 50% of the chosen step size. The piezo stage itself has a positioning accuracy of \( \approx 0.1 \text{ nm} \). Because of this choice of parameters, the presence of the cell interface itself hardly influences the bead’s fluctuations and therefore does not affect the results of the diffusion analysis. This is further supported by computer simulations shown in Figs. S4–S6.

The membrane of a living cell or a GUV is not rigid but is subject to thermal fluctuations. We have estimated the membrane fluctuations in two different ways: first, by trapping and calibrating the membrane in a weak laser focus and recording its thermal fluctuations analogously to the bead’s motion as described in (53); second, by recording the fluctuations of a 1 \( \mu \text{m} \) bead that was bound to the membrane. Both methods gave an estimate that the membrane fluctuations are in the range of 4 nm, which is five times smaller than the step size, so that we can conclude that the role of the membrane fluctuations is negligible in this study.

However, because the PCM at the outside of the cell membrane gets first into contact with the bead, it might reduce the bead’s position fluctuation width \( \sigma \). In this way \( \sigma \) might drop off to 50% before the bead touches the membrane. Therefore, we estimated the latest-possible (worst-case) contact point, where the bead fluctuations reach a minimum \( \sigma_{\text{min}} \) of around typically 30% to 40% of the bulk value \( \sigma_0 \). The alternative contact point, where the bead fluctuation is minimal, is, in average, 0.22 \( \mu \text{m} \) \( \pm \) 0.09 \( \mu \text{m} \) behind our initial contact estimate for the cells. It is likely that the true contact point between bead and cell membrane is in between these two estimates.

#### Reliability of the local viscous drag measurements

As described in the methods section, the values of the local viscous drag \( \gamma(d) \) were obtained by the AC of the measured bead’s trajectory on a short timescale of \( \tau < 30 \mu \text{s} \). As the AC is calculated from a vast number of data points, corresponding to roughly 100 times the AC time \( \tau_0 \), the results obtained from linear fitting are statistically reliable. Besides our short time analysis based on Eqs. 4 and 9, we have tested other methods to recover \( \gamma \) and \( \kappa \), such as the analysis of the complete exponentially decaying AC, of the mean square displacement, or of the PSD. All methods yielded the same results for \( \kappa_j(d) \) and \( \gamma_j(d) \) (not shown). As mentioned above, the \( \gamma \) values extracted from AC \( \tau \ll \tau_0 \) coincide well with the theoretically predicted behavior of \( \gamma \) close to a glass interface according to Happel and Brenner. A frequency resolved analysis of \( \gamma_0(\omega) \), shown in Fig. S12, reveals that \( \gamma_0(d) \) has no relevant frequency-dependent contribution and that taking the average over all frequencies \( \omega \) is justified. However, particle fluctuations nearby the cell membrane can be damped because of the PCM (glycocalyx) (8), which is not visible with DIC. This is possibly the reason for the decay of the perpendicular fluctuation width over a distance of \( \approx 0.2 \mu \text{m} \) in Fig. 3 C and the slight increase in the stiffness \( \kappa_j \) over the last 0.1 \( \mu \text{m} \) before cell contact as shown in Fig. 4 A. This length may be an indication for the thickness of the glyocalyx. Nevertheless, it is significantly shorter than the hydrodynamic decay length measured for several cells, the GUV, and the glass surface.

#### Influence of transient binding to the glyocalyx

on the fluctuation data

Figs. 3 B, and 4 both contain hints that transient binding to the PCM can be identified in the fluctuation data. In Fig. 3 B, a drop of the fluctuation width in approach direction (y) can be observed already at roughly 250 nm before contact point (0.75 \( \mu \text{m} \) > \( d \) > 0.5 \( \mu \text{m} \)), whereas the drop-off to 50% × \( \sigma_{0y} \) because of steric interaction between bead and cell is expected to take place only within one fluctuation width of
the bead, which is $\sigma_0 = 9.5$ nm in this study. This is further discussed in connection with Fig. S7.

It has been reported (8) that the PCM is not deformed or compressed by optically trapped beads passing through the PCM toward the cell membrane. Rather, the bead penetrates the PCM that thereon recovers in the vicinity of the bead. The transient binding to the PCM may reduce the fluctuation width as seen in Fig. 3 B, such that the drop to 50% of the bulk value $\sigma_0$ is reached before the actual contact with the cell membrane. By using an alternative estimate of the contact point, where $\sigma_0$ is reduced to the minimum width of $-0.3\sigma_0$ to 0.4$\sigma_0$, the hydrodynamic decay lengths $\Lambda_\parallel$ and $\Lambda_\perp$ are slightly decreased in average by 9% and 12%, respectively. At the same time, the viscous drags $\gamma_{0\parallel}$ and $\gamma_{0\perp}$ are increased in average by 40% to 63% and even 62% to 131% in the perpendicular case. However, even this worst-case estimation does not affect the overall analysis, data interpretation, and message of our study.

In Fig. 4, a rise of the stiffness parameter $\kappa_f(d)$ in approach direction of up to 20% is observed at roughly 0.1 $\mu$m before contact. Interaction with filopodia is unlikely according to the argumentation around Fig. 5, as there is no jump in $\gamma_f(d)$ (or in the parallel directions) at the same time. Also, Figs. S12 and S13 show sample approach traces for the glass interface and the GUV, which, in contrast to the cell approach, do not show a change in $\kappa_f(d)$ before the contact point.

Alongside Fig. S16, a passive microrheological analysis of the data in Fig. 4 is shown to estimate whether the transient binding to the PCM corrupts the measurement of $\gamma_f(d)$ and the associated hydrodynamic decay lengths. This becomes possible by calculating $\kappa$ and $\gamma$ from the real and imaginary part of the complex shear modulus, respectively, through the Kramers and Kronig relations. A comparison of the results obtained from AC analysis in Fig. 4 with the fluctuation range of the data obtained by microrheology (see Fig. S16) brings us to the conclusion that the determination of $\gamma_f(d)$ and $\Lambda_f$ is still valid despite the apparent interaction of the bead with the PCM. Other studies, e.g., (8,51), show how bead-optical tweezers-assays can be used to probe the structure of the PCM, which is however beyond the scope of this study.

**Error estimation for tracking nearby cells**

As pointed out in the derivation of Eq. 9, the additional signal $S_{\text{inc}}(d)$ generated by the cell leads to an apparent additional particle displacement. This optical effect leads to a wedge function with axis intercept $\Delta g_f$ adding up to the undisturbed AC and thereby slightly changing its slope and the resulting $\gamma_f(d)$. We roughly estimate from Fig. 3 A that the mean particle displacement is shifted by maximum $\Delta g_f = 50$ nm when in close proximity to the cell membrane, which is a worst-case assumption, as the actual mean shift is always below 50 nm. It follows from geometrical considerations that the additional slope can be expressed as $\Delta AC/\tau_{\text{max}} = \Delta g_f/\tau_{\text{mes}}$, where the linear part of the AC has been analyzed up to $\tau_{\text{max}} = 30$ $\mu$s and $\tau_{\text{mes}} = 150$ ms represents the measurement time at a distance $d$. Given these values, Eqs. 3 and 9 together with $\gamma_f = S_{\text{inc}}(d = R)\gamma_f$, then provide an upper limit estimate of the systematic error: $(k_B T/\gamma_{\text{max}}) = (k_B T/\gamma_f) + (\Delta g_f/\tau_{\text{mes}})$. Assuming $\gamma_{\text{max}} = \gamma_\infty = 8.0 \times 10^{-9}$ Ns/m results in $\Delta \gamma_{\text{max}} = -2.4 \times 10^{-10}$ Ns/m, which is only 3.0% of $\gamma_\infty$ (with $\Delta \gamma_{\text{max}} = \gamma_\infty - \gamma_{\text{max}}$). In conclusion, the systematic error originating from the additional signal $S_{\text{inc}}(d)$ is negligibly small in the short-time AC analysis based on Eqs. 3 and 9.

**Suitability of the exponential model**

Our simplified assumption of the exponentially decaying viscous drag for decreasing distance between the particle and the cell membrane fits remarkably well to our measurement data. It offers the great advantage that the changing hydrodynamics at smooth interfaces such as the lipid membranes of different cells or of artificial vesicles can be described by just two quantities, the maximum viscous drag $\gamma_{0\parallel}$ and the hydrodynamic decay length $\Lambda_f$. Furthermore, a comparison between viscosities at different interfaces becomes easily possible.

However, the exponential decay fails to give a correct approximation of the diffusive behavior of a bead close to a glass interface. In the right inset of Fig. 6 A, the deviation of the data points from the exponential behavior can be seen, which may lead to a misinterpretation of the calculated hydrodynamic decay lengths and MFPT for glass. A realistic estimation of the MFPTs at glass interfaces could be achieved by the numerical integration of Eq. 5 as discussed in the results section. Calculation of the MFPTs at a glass interface by using the approach of Eqs. 2 and 5 would result in $t_{\parallel}(3R,2R) = 1.016 \times t_0$ and $t_{\perp}(3R,2R) = 1.024 \times t_0$, which is unrealistically low because of the non-exponential increase of $\gamma_f(d)$ at a glass interface. The realistic results ($t_{\parallel,\text{Glass}}(3R,2R) = 0.302$ s = 1.291 $\times t_0$ and $t_{\perp,\text{Glass}}(3R,2R) = 0.417$ s = 1.782 $\times t_0$) for the MFPT, which are given in the results section, are in fact significantly higher than $t_{\parallel}(3R,2R) = 1.016 \times t_0$ and $t_{\perp}(3R,2R) = 1.024 \times t_0$.

The increase of the static viscous drag close to a plane membrane separating two identical fluids as predicted theoretically by Lee et al. (13,14) and Bickel (15,16) is of the form $\gamma(d)/\gamma_0 = (1 - \alpha (R/d))^{-1}$ and does not resemble an exponentially decaying function ($\alpha$ is a constant and $R$ is the sphere radius). However, a bead close to a spherical surface—like it is the case for our cells—can drag the water more easily to the side, compared with the case of a plane surface. Therefore, one can expect a less-steep increase in viscous drag close to a spherical surface, which could partly explain the difference between our measured curves and the theoretical predictions for the static viscous drag. However,
further investigations are required to model the decay of the viscous drag considering dynamic effects, nonplane and elastic membranes, as well as different viscosities on both sides of the membrane.

Anisotropy of hydrodynamic decay lengths for living cells

All measurements performed on cells show the common result that the hydrodynamic decay lengths in perpendicular direction are significantly longer than in parallel direction. This behavior cannot be seen with the GUV, where \( A_\perp \) and \( A_\parallel \) are of comparable length. Interestingly, GUVs and cells, which both have a phospholipid bilayer membrane, show the same decay lengths of \( A_\parallel \approx 0.3 \) \( \mu \)m for parallel diffusion.

A possible physical explanation for a significantly stronger increase in viscous drag for perpendicular diffusion could be the following: without an interface, the hydrodynamic drag can be transferred from one particle to another via the surrounding fluid, depending on the distance (10,54). A transfer of hydrodynamic momentum through an interface is also possible, if the interface can deform and relax its shape or can transmit fluid molecules to a certain extent. Lipid membranes behave like this, and therefore can transfer hydrodynamic momentum from the outside of the GUV to its interior, i.e., in normal direction equally well as in lateral direction. In front of a stiff wall the hydrodynamic drag cannot be transferred anymore, which leads to a local fluid compression. In consequence, the motion of a bead is hindered and damped, leading to a strong increase in viscosity; see Fig. 6 B. Simply because of geometric constraints, it is obvious that the fluid can be dragged more easily parallel to the interface than in direction to the interface. This coincides with the theoretical prediction that the normal component of the viscous drag close to a glass surface increases to infinity with decreasing distance according to the theory of Happel and Brenner, i.e., \( \gamma_{\perp} \to \infty \), but also diverges in the experiments. Unlike solid surfaces, lipid membranes behave like two-dimensional fluids and a hydrodynamic drag from the environment can result in lateral membrane motion, thus reducing friction in parallel direction.

The hydrodynamic momentum produced by the drag of the sphere is completely repelled at a stiff interface, thus doubling the amount of mechanical momentum taken up by the stiff medium. A thin elastic membrane transfers most of the incoming momentum without significant repulsion. Cells represent an intermediate case, where part of the momentum is transferred and the other part is repelled, leading to an increase in viscous drag with a specific decay length. This hydrodynamic coupling length is the distance within which the momentum transfer to the interface starts to increase relative to the case of a homogeneous fluid.

At the cell membranes, the perpendicular drag coefficients \( \gamma_{\perp} = 5.1 \times \gamma_{\perp} \) (J774) and \( \gamma_{\perp} = 6.2 \times \gamma_{\perp} \) (HT29) are five to six times larger than the bulk value \( \gamma_\perp = 8.0 \times 10^{-9} \) Ns/m, whereas the increase in viscous drag close to a GUV membrane is fundamentally smaller (\( \gamma_{\perp} = 1.10 \times \gamma_\perp \)). In other words, momentum transfer through a membrane is better possible, if the fluid on both sides of the membrane is approximately the same regarding viscosity and osmolarity, as in the case of the GUV. However, the situation is different with living cells, because the plasma membrane exhibits a more complex composition of different lipids and lipid rafts, pores, and membrane proteins, many of them linked to the cytoskeleton (55). The interior of the cell is crowded with vesicles, macromolecules, cytoskeletal filaments, organelles, and other membranes, resulting in a higher density and a more rigid structure that apparently dampens the transfer of hydrodynamic momentum. The difference in \( \gamma_{\perp} \) for different cell types is probably a result of different compositions of the cell interior and also of the PCM, both because of the different functions of these cell types.

Our calculations show that the MFPTs are also influenced, as shown in Fig. 7. For a sphere diffusing over \( R = 0.5 \) \( \mu \)m toward the cell from distance \( d_1 = 3R \) toward \( d_2 = 2R \), the parallel MPFTs are hardly changed. In perpendicular direction, however, the MPFT is increased significantly by 30% to 65%. These times become the longer, the closer the particle approaches the cell.

Biological interpretation

The hydrodynamic coupling of the approaching particle in perpendicular direction exerts a hydrodynamic pressure, i.e., momentum transfer, onto the cell, which, in consequence, must apply a force to the membrane and mechano-sensitive proteins therein. The pronounced increase in viscous drag slows down the particle’s diffusion and thus reduces the rate of collisions with membrane components and thereby reduces the interaction probability in a given time window. The denser and more viscous the cell, the more hydrodynamic momentum is transferred to its interior, but the more the mobility and the collision rate are reduced outside the cell. The reduced collision rate corresponds to a limited temporal bandwidth of information (momentum) transfer. In this way, less broad-band noise is transferred to the cell. Thereby, the local increase of viscosity leads to a low-pass filtering of incoming signals, and one may conclude that only distinct, pronounced momentum changes can be transferred to the cell interior.

For example, as a response to the hydrodynamic pressure of the particle, the cell can reorganize the cytoskeleton connected to the membrane or can initiate the growth of cell protrusions such as filopodia. The larger parallel mobility compared with the bead’s perpendicular motion allows a particle to diffuse faster parallel to the membrane and to better find specific or unspecific binding sites across the cell surface. Because the particle fluctuations are faster in parallel than in
perpendicular direction, also the particle’s collision rate is higher in parallel direction. This might, for example, help cells to improve their endocytosis efficiency by a facilitated search of the particle for membrane binding sites.

CONCLUSIONS
The viscosity of a fluid determines the mobility of a particle on a macroscopic scale and the dissipation of particle fluctuations on a microscopic scale. Close to different cellular interfaces, this behavior changes strongly—an effect that can significantly influence the probability of particle binding to the interface. Using a photonic force microscope with a fast 3D interferometric particle tracking system, we show for the first time, to our knowledge, that the viscous drag increases nearly exponentially with decreasing distance to the membranes of living cells and of GUVs. Similar to the direction-dependent changes of the viscosity nearby stiff interfaces, but nevertheless unexpected, we found that three different types of cells show a significantly stronger increase in viscosity in perpendicular direction than in parallel direction. However, all three different cells and the GUVs are characterized by a strongly different hydrodynamic coupling length and maximum viscosity, which we believe are a consequence of the cell’s composition and its regulation of proteins and lipids inside the cell or the membrane and also the PCM. It is remarkable that the correlation of the particle position fluctuations encode the cellular membrane composition and the ability to transfer information. However, further investigations need to uncover the relation between the cellular constituents near the membrane, the hydrodynamic coupling length and strength outside the membrane, and the connected physiological function. Fast particle fluctuations, as measurable by photonic force microscopy, encode a lot of relevant information to understand the molecular processes of endocytosis or drug delivery.

SUPPORTING MATERIAL
Supporting Material, sixteen figures, and three tables are available at http://www.biophysj.org/biophysj/supplemental/S0006-3495(15)00734-1.

AUTHOR CONTRIBUTIONS
F.J. performed cell experiments, analyzed and interpreted the data, and prepared the figures; F.K. designed and constructed the microscope setup; A.M. performed GUV experiments; T.M. developed the BD simulation framework; R.N. and B.E. provided and prepared the cells; and A.R. initiated and supervised the project, obtained financial funding, interpreted the data, and wrote the manuscript together with F.J.

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SUPPORTING CITATIONS
References (56–60) appear in the Supporting Material.

REFERENCES


